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## **CLAIMS**

- 1. Equalization method for the cancellation of isofrequential interferers in signals received by array antennas (ARY) of base stations of a cellular mobile system, said signals (y(n)) being received under the form of bursts of data symbols of a transmission burst, including a training sequence  $(\{x_n\})$  known to the receiver and usable to estimate the impulse response of the transmission channel, said bursts received being demodulated, digitized, stored, and synchronized through discrimination of the training sequence, including the following steps:
- a) spatial filtering of signals coming from the antennas (y(n)), using a spatial filter (BMF) that combines among them corresponding n-th symbols of the bursts on the basis of n-th weights of a sequence of weights  $(\mathbf{w}_{opt}(n))$  obtaining a beamformed received sequence  $(\mathbf{y}_{out}(n))$ ;
- b) time filtering (CAMP) data of the training sequence  $(\{x_n\})$  for estimating a sequence of samples (h(n)) of the impulse response of the transmission channel;
- c) calculating a square error  $(e_n)$  originated from the comparison between the corresponding n-th samples of the estimate impulse response  $(\mathbf{h}(n))$  and the beamformed sequence  $(\mathbf{y}_{out}(n))$ ;
  - d) joint optimization of said weights and samples  $\left(\mathbf{w}_{opt}(n), \mathbf{h}_{opt}(n)\right)$  by minimizing a functional (FUNZ) corresponding to said mean square error  $\left(e_{n}\right)$ ;
- e) time filtering of the signal  $(y_{out}(n))$  generated by said spatial filter (BMF) using a filter (FADAT) matched to the sequence of samples  $(\mathbf{h}_{opt}(n))$  of the impulse response of the transmission channel;
  - f) providing said sequence of samples of the impulse response of the transmission channel  $(\mathbf{h}_{opt}(n))$  and a sequence of sample at the output of said matched filter (FADAT) to a Viterbi estimator for the detection of the received data;
  - g) updating the optimized values of said weights and samples  $(\mathbf{w}_{opt}(n), \mathbf{h}_{opt}(n))$ , out of the time slot of the training sequence, through repetition of the previous steps

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a)...f), replacing the symbols of the training sequence  $(\{x_n\})$  by a low delay estimated sequence  $(\{\hat{x}'_n\})$ , thus rendering said equalization adaptive,

characterized in that while the previous steps are executed a parallel continuous monitoring of the power received on the antennas (ARY) for detecting possible peaks exceeding a given threshold in coincidence of the arrival of a strong non-stationary interferer is carried out, in case of detection of a peak over threshold at an instant  $\overline{n}$ , step d) is modified for the all duration starting from the instant  $\overline{n}$  up to an instant  $\overline{n} + \Delta T$  of a transient devoted to the rejection of strong interferent outside the midamble, by updating the sole weights  $(\mathbf{w}_{opt}(n))$  of the spatial filter (BMF) maintaining the samples of the impulse response  $(\mathbf{h}_{opt}(n))$  constant at the values they have at the instant  $\overline{n}$ , then the execution of unmodified step d) is restored at the end of said transient.

- 2. Equalization method according to claim 1, characterized in that in absence of a strong non-stationary interferer the preceding step d) is executed in closed form by the following sub-steps:
- calculation of a spatial covariance matrix  $\mathbf{R}_{yy}$  of the signals coming from the antennas  $(\mathbf{y}(n))$ , a covariance matrix  $\mathbf{R}_{x}$  of the data samples  $(\{x_n\}, \{\hat{x}'_n\})$ , a cross-covariance matrix  $\mathbf{R}_{xy}$  between data samples and inputs to the antennas  $(\{x_n\}, \mathbf{y}(n))$ , and the Schur complement matrix  $\mathbf{R}_{x}^{\perp} = \mathbf{R}_{xx} \mathbf{R}_{xy} \mathbf{R}_{yy}^{-1} \mathbf{R}_{xy}^{*}$ , being \* the complex conjugate, of a matrix  $\mathbf{R} = \begin{bmatrix} \mathbf{R}_{yy} & \mathbf{R}_{xy}^{*} \\ \mathbf{R}_{xy} & \mathbf{R}_{xy} \end{bmatrix}$ ;
- estimation of an eigenvector  $\mathbf{h}_{opt}(n)$  of matrix  $\mathbf{R}_{s}^{\perp}$  associated to the minimum module eigenvalue  $\gamma$  given by  $\mathbf{h}^{\bullet}\mathbf{R}_{s}^{\perp}\mathbf{h} = -\gamma$ , said eigenvector including said optimized samples;
- estimation of said optimized weights by calculating a vector  $\mathbf{w}_{opt}(n)$  solution of the equation:  $\mathbf{R}_{yy}\mathbf{w}_{opt}(n) = \mathbf{R}_{xy}^{\bullet}\mathbf{h}_{opt}(n)$ .
  - 3. Equalization method according to claim 1, characterized in that in presence of a strong non-stationary interferer the preceding step d) is executed in closed form by the following sub-steps:

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- calculation of a spatial covariance matrix  $\mathbf{R}_{_{\mathcal{P}}}(\overline{n}+\Delta T)$  of the signals coming from the antennas  $(\mathbf{y}(n))$  and a complex conjugate cross-covariance matrix  $\mathbf{R}_{_{\mathcal{P}_{N}}}^{\bullet}(n)$  between data samples and inputs to the antennas  $(\{x_n\},\mathbf{y}(n))$ , matrix  $\mathbf{R}_{_{\mathcal{P}_{N}}}(\overline{n}+\Delta T)$  being calculated at instant  $\overline{n}$ , and then kept constant for the whole  $\Delta T$ , using vectors  $\mathbf{y}(n)$  obtained from the samples of signals on the antennas present in the stored bursts, starting from instant  $\overline{n}$  up to the instant  $\overline{n}+\Delta T$ , while  $\mathbf{R}_{_{\mathcal{P}_{N}}}^{\bullet}(n)$  being calculated at each instant n-th of the transient;
- estimation of said optimized weights by calculating a vector  $\mathbf{w}_{opt}(n)$  solution of the equation:  $\mathbf{R}_{yy}(\overline{n} + \Delta T)\mathbf{w}_{opt}(n) = \mathbf{R}_{xy}^*(n)\overline{\mathbf{h}}_{opt}$ , where  $\overline{\mathbf{h}}_{opt}$  is a vector including the samples of the impulse response at the instant  $\overline{n}$ .
- 4. Equalization method according to claim 1, characterized in that in absence of a strong non-stationary interferer the preceding step d) is executed in iterative form by the following sub-steps:
- d1) assignment of arbitrary values, preferably null, to the elements of a structured triangular matrix  $\overline{\mathbf{L}}(n)$ , defines as follows:  $\overline{\mathbf{L}}(n) = \begin{bmatrix} \mathbf{L}(n) & \mathbf{0} \\ \mathbf{U}(n) & \mathbf{L}_s(n) \end{bmatrix}$ , wherein  $\mathbf{L}(n)$  and  $\mathbf{L}_s(n)$  are triangular matrices and  $\mathbf{U}(n)$  is a square matrix, or more in general a rectangular one;
  - d2) assignment of arbitrary values, one of which non null, to the elements of a vector  $\mathbf{h}_{opt}(n)$  storing said optimized samples of the impulse response of the transmission channel;
  - d3) assignment of arbitrary values, one of which at least non null, to the elements of a vector  $\mathbf{w}_{opt}(n)$  storing said weights of the spatial filter (BMF);
- d4) updating of said structured matrix  $\overline{\mathbf{L}}(n)$  applying at instant n-th the following iterative relation:  $\left[\overline{\mathbf{L}}(n) \quad \mathbf{0}\right] = \left[\overline{\mathbf{L}}(n-1) \quad \mathbf{g}_n\right] \mathbf{Q}(n)$ , where  $\mathbf{g}_n$  is the following updating vector  $\mathbf{g}_n = \begin{bmatrix} \mathbf{y}(n) \\ \mathbf{x}(n) \end{bmatrix}$  structured in two component vectors, out of which:  $\mathbf{y}(n) = \begin{bmatrix} y_1(n), y_2(n), \dots, y_M(n) \end{bmatrix}^T \text{ is a first vector whose } M \text{ elements are symbols coming from } M \text{ antennas at instant } n\text{-th, present in a same number of stored}$

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bursts, and  $\mathbf{x}(n) = \begin{bmatrix} x_n(n), x_{n+1}(n), \dots, x_{n+L-1}(n) \end{bmatrix}^T$  is a second vector whose L elements are stored symbols of the transmitted training or estimated sequence  $\left( \left\{ x_n \right\}, \left\{ \hat{x}^i_{\ n} \right\} \right)$  respectively, assuming a duration of the impulse response equal to L symbols; being  $\mathbf{Q}(n)$  a matrix transformation of unitary rotation, implemented through a sequence of elementary transformations  $\mathbf{Q}_0, \mathbf{Q}_1, \cdots$ , that applied to  $\left[ \overline{\mathbf{L}}(n-1) \ \mathbf{g}_n \right]$  produces the cancellation of column  $\mathbf{g}_n$  introducing a zero for each elementary transformation;

- d5) determination of a weight vector  $\mathbf{h}_n$  through the following expression:  $\mathbf{L}_s(n)\mathbf{L}_s^*(n)\mathbf{h}_n = \mathbf{h}_{opt}(n-1), \text{ according to which said vector of optimum}$  samples is updated as follows  $\mathbf{h}_{opt}(n) = \frac{\mathbf{h}_n}{\mathbf{h}_n^*\mathbf{h}_n}$ ;
- d6) updating of said optimum weight vector through the following expression:  $\mathbf{L}^{*}(n)\mathbf{w}_{opt}(n) = \mathbf{U}^{*}(n)\mathbf{h}_{opt}(n).$
- 5. Equalization method according to claim 4, characterized in that said expression calculated at step h5) is divided into two calculation phases, introducing an unknown intermediate vector  $\mathbf{u}_n$  defined by the following first equation:  $\mathbf{L}_s^*(n)\mathbf{h}_n = \mathbf{u}_n$ , being  $\mathbf{u}_n$  a solution of the following second equation:  $\mathbf{L}_s(n)\mathbf{u}_n = \mathbf{h}_{opt}(n-1)$  that replaced in its turn in the starting equation gives  $\mathbf{h}_n$ , simplifying the relevant calculation.
- 6. Equalization method according to claim 4, characterized in that said matrix  $\overline{\mathbf{L}}(n-1)$  is multiplied by  $\sqrt{\lambda}$ , where  $\lambda$  is an arbitrary real constant, lower than one unit, selected in relation to the non stationariness of the channel.
  - 7. Adaptive equalization method according to claim 1, characterized in that, in presence of a strong non-stationary interferer the preceding step d) is executed in iterative form by the following sub-steps:
- 25 h1) advanced updating within the symbol time  $\overline{n}$  of a sole triangular matrix L belonging to a structured triangular matrix  $\overline{L}(n)$ , defined as follows:  $\overline{L}(n) = \begin{bmatrix} L(\overline{n} + \Delta T) & 0 \\ U(n) & L_s(n) \end{bmatrix}$ , wherein  $L(\overline{n} + \Delta T)$  and  $L_s(n)$  are triangular matrices and U(n) is a square matrix, or more in general a rectangular one; the advanced

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updating of said matrix  ${\bf L}$  being executed using vectors  ${\bf y}(n)$  obtained from the samples of signals on the antennas, present in the stored bursts, starting from instant  $\overline{n}$  up to an instant  $\overline{n}+\Delta T$ ; matrix  ${\bf L}$  being calculated at instant  $\overline{n}$  and then kept constant for the whole  $\Delta T$ ;

- 5 h2) starting from instant  $\overline{n}$  up to an instant  $\overline{n} + \Delta T$ , updating of matrices U(n) and  $L_s(n)$  of said triangular matrix  $\overline{L}(n)$  applying at instant n-th the following iterative relation:  $\left[\overline{L}(n) \quad \mathbf{0}\right] = \left[\overline{L}(n-1) \quad \mathbf{g}_n\right] \mathbf{Q}(n)$ , where  $\mathbf{g}_n$  is the following updating vector  $\mathbf{g}_n = \begin{bmatrix} \mathbf{y}(n) \\ \mathbf{x}(n) \end{bmatrix}$  structured in two component vectors, out of which:
  - $\mathbf{y}(n) = \begin{bmatrix} y_1(n), y_2(n), \dots, y_M(n) \end{bmatrix}^T$  is a first vector whose M elements are symbols coming from M antennas at instant n-th, present in a same number of stored bursts, and  $\mathbf{x}(n) = \begin{bmatrix} x_n(n), x_{n+1}(n), \dots, x_{n+L-1}(n) \end{bmatrix}^T$  is a second vector whose L elements belong to said low delay estimated sequence  $\left( \left\{ \hat{x}'_n \right\} \right)$ , assuming a duration of the impulse response equal to L symbols; being  $\mathbf{Q}(n)$  a matrix transformation of unitary rotation, implemented through a sequence of elementary transformations  $\mathbf{Q}_0, \mathbf{Q}_1, \dots$ , that applied to  $\left[ \overline{\mathbf{L}}(n-1) \ \mathbf{g}_n \right]$  produces the cancellation of column  $\mathbf{g}_n$  introducing a zero for each elementary transformation;
  - h3) updating of said optimum weight vector through the following expression:  $\mathbf{L}^{\bullet}(\overline{n} + \Delta T)\mathbf{w}_{opt}(n) = \mathbf{U}^{\bullet}(n)\overline{\mathbf{h}}_{opt}, \text{ where } \overline{\mathbf{h}}_{opt} \text{ is a vector including the samples of the impulse response at the instant } \overline{n}.$
  - 8. Equalization method according to claim 7, characterized in that said advanced updating of the sole triangular matrix L, is made applying the generic said elementary transformation  $Q_i$  to the first M elements of the i-th column of said triangular matrix  $\overline{L}(n)$ , where M is the order of matrix L, repeating the elementary transformation  $Q_i$  for all the values of index i and storing the transformations occurred.
- 9. Equalization method according to claim 7 or 8, characterized in that said matrix  $\overline{L}(n-1)$  is multiplied by  $\sqrt{\lambda}$ , where  $\lambda$  is an arbitrary real constant, lower than one unit, selected in relation to the non stationariness of the channel.
  - a 10. Equalization method according to A ene of the previous claims,

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characterized in that, coinciding with any new symbol of low delay estimated sequence  $(\{\hat{x}'_n\})$ , the L elements of said vector  $\mathbf{x}(n)$  are replaced by a same number of symbols copied as a whole from the path selected in the trellis at the present symbol time, preventing by this the propagation of errors in the joint estimate of said optimum weights and channel impulse response samples  $(\mathbf{w}_{opt}(n), \mathbf{h}_{opt}(n))$ .

- 11. Equalization method according to n any of the preceding claims, characterized in that when said training sequence  $(\{x_n\})$  is included in a midamble of the transmission burst, said equalization of the step g) starts from a first end of the midamble and proceeds towards the end of the burst, previously stored and synchronized, and afterwards it restarts from the second end of the midamble towards the other end of the burst, using estimated data of the first semiburst to have a longer group of estimated data for the equalization of the second semiburst.
  - 12. Equalizer in receivers of base stations of a cellular mobile system, in particular for the cancellation of isofrequential interferers in signals received by array antennas (ARY) of base stations of a cellular mobile system, said signals (y(n)) being received under the form of bursts of data symbols of a transmission burst, including a training sequence  $(\{x_n\})$  known to the receiver and usable to estimate the impulse response of the transmission channel, said bursts received being demodulated, digitized, stored, and synchronized through discrimination of the training sequence, including:
  - a spatial filter (BMF) of signals coming from the antennas (y(n)) that combines among them corresponding n-th symbols of the bursts on the basis of n-th weights of a sequence of weights  $(\mathbf{w}_{opt}(n))$  obtaining a beamformed received sequence  $(y_{out}(n))$ ;
- 25 a time filter (CAMP) for filtering data of the training sequence  $(\{x_n\})$  and estimating a sequence of samples (h(n)) of the impulse response of the transmission channel;
  - means  $(\Sigma)$  suitable for calculating a square error  $(e_n)$  originating from the comparison between the corresponding n-th samples of the estimate impulse

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- response (h(n)) and the beamformed sequence  $(y_{out}(n))$ ;
- means (FUNZ) suitable for the joint optimization of said weights and samples  $\left(\mathbf{w}_{opt}(n), \mathbf{h}_{opt}(n)\right)$  and to minimize a functional (FUNZ) corresponding to said mean square error  $\left(e_n\right)$ ;
- a time matched filter (FADAT) of the signal  $(y_{out}(n))$  generated by said spatial filter (BMF), matched to the sequence of samples  $(\mathbf{h}_{opt}(n))$  of the impulse response of the transmission channel;
  - a Viterbi estimator (STIM) for estimating the symbols  $(\{\hat{x}_n\})$  of the transmission burst corresponding to the sequence coming out from the time matched filter (FADAT);
  - means (DECTEMP) suitable for replacing out of the time slot of the training sequence the symbols of the training sequence  $(\{\hat{x}_n\})$  with a low delay estimated sequence  $(\{\hat{x}_n\})$ , thus rendering said equalization adaptive,

## characterized in that it further includes:

- means (PICRIV) suitable for the continuous monitoring of the power received on the antennas (ARY) and for detecting possible peaks exceeding a given threshold in coincidence of the arrival of a strong non-stationary interferer;
  - selection means (PICSEL, SWT) controlled by said continuous monitoring means (PICRIV) suitable for the selection of said means (SYSTOL1, 3, 4, 5) for the joint optimization of weights and samples, in case a detection of a peak over threshold doesn't occur, and for the selection of means (SYSTOL2, SYSTOL5) devoted to the rejection of a strong interferent in case of detection of a peak over threshold occur at an instant  $\bar{n}$  outside the midamble; the latter means being operative for the all duration starting from the instant  $\bar{n}$  up to an instant  $\bar{n} + \Delta T$  of a rejecting transient and being arranged for updating the sole weights  $(\mathbf{w}_{opt}(n))$  of the spatial filter (BMF) maintaining the samples of the impulse response  $(\mathbf{h}_{opt}(n))$  constant at the values they have at the instant  $\bar{n}$ ; the preceding means for the joint optimization (SYSTOL1, 3, 4, 5) being restored at the end of said rejection transient.
    - 13. Equalizer according to claim 12, characterized in that in absence of strong

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or square;

non-stationary interferer said joint optimization means (SYSTOL1, 3, 4, 5) are constitute by the following means:

- first delay means (RIT) for delaying with a fixed delay (D) an algebraic vector  $\mathbf{y}(n)$  of M elements, as many as the antennas, whose elements are symbols of the stored bursts of the signal coming from the antennas;
- a first systolic array (SYSTOL1) receiving said vector  $\mathbf{y}(n)$  and symbols of said training sequence  $\left(\left\{x_n\right\}\right)$  or estimated low delay ones, organized as in an algebraic vector  $\mathbf{x}(n)$  of L elements, equal to the length of the channel impulse response, and updating, coinciding with each symbol time n-th, a triangular matrix  $\overline{\mathbf{L}}(n) = \begin{bmatrix} \mathbf{L}(n) & \mathbf{0} \\ \mathbf{U}(n) & \mathbf{L}_s(n) \end{bmatrix} \text{ image of said first systolic array (SYSTOL1) in which the elements <math>\mathbf{L}(n)$  and  $\mathbf{L}_s(n)$  are also triangular matrices, and  $\mathbf{U}(n)$  is rectangular,
- a second systolic array (AUTOVET), said second systolic array receiving said element  $\mathbf{L}_{s}(n)$  and updating a vector  $\mathbf{h}_{opt}(n)$  whose elements correspond to the optimized samples of the impulse response,
- a third systolic array (SYSTOL5), placed in cascade to the second, receiving said elements  $\mathbf{L}(n)$  and  $\mathbf{U}(n)$ , the vector  $\mathbf{h}_{opt}(n)$ , and updating a vector  $\mathbf{w}_{opt}(n)$  whose elements correspond to the optimized weights.
- systolic array (AUTOVET), is further divided in the cascade of two systolic arrays (SYSTOL3, SYSTOL4) having identical triangular structure, of which the upstream array (SYSTOL3) receives said element  $\mathbf{L}_s(n)$ , and the previous vector  $\mathbf{h}_{opt}(n-1)$  of the downstream array, and calculates an intermediate vector  $\mathbf{u}_n$  supplying it to the downstream array (SYSTOL4), reached also by element  $\mathbf{L}_s(n)$ , for the calculation of said vector  $\mathbf{h}_{opt}(n)$ .
  - 15. Equalizer according to claim 12, characterized in that in presence of strong non-stationary interferer said joint optimization means (SYSTOL2, SYSTOL5) are constitute by the following means:
- first delay means (RIT) for delaying with a fixed delay (D) an algebraic vector  $\mathbf{y}(n)$ of M elements, as many as the antennas, whose elements are symbols of the

stored bursts of the signal coming from the antennas;

- a first systolic array (SYSTOL2) receiving said vector  $\mathbf{y}(n)$  and the symbols of said low delay estimated sequence  $\left(\left\{\hat{x}'_n\right\}\right)$  organized as in an algebraic vector  $\mathbf{x}(n)$  of L elements, equal to the length of the channel impulse response, and updating,
- coinciding with each symbol time n-th, a matrix  $\overline{\mathbf{L}}(n) = \begin{bmatrix} \mathbf{L}(\overline{n} + \Delta T) & \mathbf{0} \\ \mathbf{U}(n) & \mathbf{L}_s(n) \end{bmatrix}$  image of said first systolic array (SYSTOL2) in which the elements  $\mathbf{L}(n)$  and  $\mathbf{L}_s(n)$  are also triangular matrices, and  $\mathbf{U}(n)$  is rectangular or square matrix;
  - second delay means (FIFO) suitable for delay element  ${f L}$  calculated at instant  ${f n}$  for the whole  ${\it \Delta}T$ ;
- a second systolic array (SYSTOL5), placed in cascade to the first, receiving said elements  $\mathbf{L}(n)$  and  $\mathbf{U}(n)$ , a vector  $\overline{\mathbf{h}}_{opt}$  including the samples of the impulse response at the instant  $\overline{n}$ , and updating a vector  $\mathbf{w}_{opt}(n)$  whose elements correspond to the optimized weights
- 16. Equalizer according to claim 13 er-15, characterized in that said vectors  $\mathbf{y}(n)$  and  $\mathbf{x}(n)$  reach in column, in the order indicated, the input of the cells of said first systolic array (SYSTOL1, SYSTOL2) corresponding to the elements of the first column of said matrix  $\overline{\mathbf{L}}(n)$ , the whole of cells of the triangular matrix including the calculation means of the following matrix relation:

$$\begin{bmatrix} \alpha & out \end{bmatrix} \leftarrow \begin{bmatrix} \alpha \sqrt{\lambda} & in \end{bmatrix} \frac{1}{\sqrt{1+|\rho|^2}} \begin{bmatrix} 1 & \rho \\ \rho^* & -1 \end{bmatrix}$$

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- $\alpha$  pointed by the arrow indicates the new content of the cell;
- λ is an arbitrary real constant ≤ 1, selected in relation to the non stationariness of the channel.
- out is an output signal;
- 25 in is a signal entering each cell; and
  - p is a both input and output signal, calculated as follows:

$$\rho = \frac{in}{\alpha\sqrt{\lambda}};$$

the cells corresponding to the elements of the main diagonal of said matrix  $\overline{\mathbf{L}}(n)$ 

containing the alternative calculation means, such for which the signal  $\rho$  is only an output one, the signal out is absent, and the content  $\alpha$  is updated as follows:

$$\alpha \leftarrow \sqrt{\lambda |\alpha|^2 + |in|^2} .$$